MATHEMATICAL MODEL AND OPERATION MODES OF DRUM-TYPE BIOFERMENTER

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Abstract. One of the most effective technologies for manure utilization is its processing in a drum bio-fermenter. This technology allows obtaining different products with specified end-use properties in the same installation depending on the operation mode. The created mathematical model is designed to determine the modes, under which the bio-fermentation processes in the processed material are most intensive and feature the least nutrients loss. The model input factors were aeration time (from 3 to 7 min·h⁻¹ per one ton), aeration rate (from 5.5 to 9.5 m·s⁻¹ under the 76 mm pipeline diameter) and drum rotation frequency (three rotations every 6 to 12 hours). The target function was the product temperature reached in the bio-fermenter during manure processing. Experiments with three replications were carried out in the laboratory of bioconversion of organic waste in IEEP on a patented drum bio-fermenter. The starting material was separated solid fraction of cattle manure. Based on the calculation results the error of experiment reproducibility was 1.85. The developed mathematical model allows establishing the effect of individual input factors and their combinations on the target function. After the model analysis the pair interaction of time and aeration rate factors were found to have the most sizable contribution to the temperature variation in the bio-fermenter. The rational modes of drum bio-fermenter operation were identified to obtain different end products with desired properties and to further optimize the conversion process.

Key words: manure, bio-fermentation, mathematical model, drum bio-fermenter, ecology.

Introduction

Livestock production is directly associated with manure formation. Every year its utilisation is becoming an increasingly significant problem. In the North-West of the Russian Federation composting is the basic manure utilisation technique. It allows to obtain the high quality organic fertilizer, which forms the basis for extension of the humus layer of soil and subsequent increase of crop yields [1].

Intensification of livestock industry toughens the requirements for the manure utilization technology forcing to introduce new, faster and more efficient processing practices. One such technology is accelerated manure composting in a drum bio-fermenter.

The basic condition for successful composting is to provide the microorganisms, involved in aerobic fermentation of manure, with the most comfortable living conditions: sufficient amount of oxygen and optimum temperature [2]. Specific design features of a drum bio-fermenter allow to vary its operation modes in order to receive different products with desired final properties: organic fertilizers or bedding for farm animals [3; 4].

The aim of the work was to create a mathematical model of a drum bio-fermenter and to determine the rational modes of its operation to produce bedding and fertilizers.

Materials and methods

The study was conducted in 2015-2016 in the IEEP Organic Waste Bioconversion Laboratory on a patented drum-type bio-fermenter (Fig. 1) [5]. Bio-fermenter is a revolving drum with insulating coating, mounted on a fixed frame with the help of rollers. The driving system includes the power unit and the motor reduction unit. The aeration system of the composted mass is a perforated pipe placed inside the drum along its full length. Special blades are evenly spaced around the inner diameter of the drum to direct the ready compost to the discharging auger.

The laboratory-scale model of the bio-fermenter with the dimensions of 4300x2100x1650 mm, effective capacity of 2.2 m³, and the daily output of 0.7 m³, allows to investigate the biofermentation process of different types of organic waste in the real time mode.

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Initial raw material in the study was solid fraction of cattle manure from a dairy farm with the animal stock of 900 heads, manure output of $90 \text{ m}^3\text{·day}^{-1}$ and the system of manure separation into solid and liquid fractions in place.

The raw material and final product were analysed in the analytical laboratory of IEEP.

The experiment was conducted under a cyclic operation mode of the bio-fermenter with three replications. The experimental design technique [6] was implemented in the study, with the optimisation factor being the self-heating temperature of the composted mass in the bio-fermenter.

Amount of the composted material of 1240 kg was taken with due account for the minimal critical mass values required for the successful conversion process [7] and the design features of the laboratory-scale bio-fermenter.

Dynamic pattern of temperature, mass, humidity and chemical composition was recorded in the real time mode. The matrix of full factorial experiment of the $2^n$ type was implemented, where $n=3$ is the number of input variables (Table 2). To improve the accuracy and reliability of the obtained results, each experiment consisted of three parallel replications. The experiments were carried out using randomization.

The following equipment was used in the experiment: Т ЦМ 9410/M2 thermometer with ±0.5 °C sensitivity; strain sensor 3410-2000-C3 with 0.02 % error; laboratory scales Pioneer with 0.005 % error; pH-meter/ionometer ЭКСПЕРТ-001 3(01) with 0.02 % error, spectrophotometer ПЭ-5400 B with the accuracy of 0.001 %, as well as atomic absorption spectrophotometer Shimadzu AA-680, with 0.001 % error.

During the experiment the ambient temperature was maintained at a constant level of 15±1 °C.

In the experiment the phenomenon of bio fermentation of organic waste was investigated in terms of creating the most favourable conditions for the development of microorganisms. The previous research has shown that from 5.2 to 7.4 m$^3$ of air are required to decompose one kg of organic matter and the method of air supply to the processed material is of great importance [8; 9]. In view of this, the input factors (independent variables) were selected, which had the strongest impact on the process of accelerated composting in a drum biofermenter: aeration time, aeration rate and drum rotation interval. Table 1 presents the variability intervals of independent variables, with the accepted measurement units being indicated.

<table>
<thead>
<tr>
<th>Variable code</th>
<th>Variable name</th>
<th>Measurement unit</th>
<th>$\text{min}$</th>
<th>$\text{max}$</th>
<th>Variability interval</th>
</tr>
</thead>
<tbody>
<tr>
<td>$X_1$</td>
<td>Aeration time</td>
<td>min·h$^{-1}$</td>
<td>3</td>
<td>7</td>
<td>4</td>
</tr>
<tr>
<td>$X_2$</td>
<td>Aeration rate</td>
<td>m·s$^{-1}$</td>
<td>5.5</td>
<td>9.5</td>
<td>4</td>
</tr>
<tr>
<td>$X_3$</td>
<td>Drum rotation interval</td>
<td>Hour</td>
<td>6</td>
<td>12</td>
<td>6</td>
</tr>
</tbody>
</table>
The temperature of the composted mass in the biofermenter as an indicator of the processing intensity was accepted as dependent variable \( Y (°C) \). The properties, purpose and quality of the final product depend on the stable temperature control.

In fertilizer production the key objective is to retain the maximum amount of nutrients in the end product. Under 62.5 °C protein coagulation and degradation of nutrient compounds take place that have an adverse effect on the product quality [10]. In bedding production a more important factor is its moisture-retaining capacity. So, here the priority objective is to reduce the moisture content of the end product that is achieved through higher temperature.

Results and discussion

The matrix of the full factorial experiment is presented in Table 2.

The values of the dependent variable \( Y \) are given as the average of three parallel determinations, or which additional error of reproducibility was calculated.

Table 2 shows all independent variables in the standardised form:

\[
x_i = \frac{X_i - \bar{X}_i}{\Delta X_i}, \tag{1}
\]

where \( X_i \) and \( \bar{X}_i \) – correspondingly coded and measured values of the input variable;

\( \Delta X_i \) – variability interval.

<table>
<thead>
<tr>
<th>No.</th>
<th>Aeration time</th>
<th>Aeration rate</th>
<th>Drum rotation interval</th>
<th>Temperature in bio-fermenter</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>-1</td>
<td>-1</td>
<td>-1</td>
<td>53.17</td>
</tr>
<tr>
<td>2</td>
<td>1</td>
<td>-1</td>
<td>-1</td>
<td>72.33</td>
</tr>
<tr>
<td>3</td>
<td>-1</td>
<td>1</td>
<td>-1</td>
<td>65.60</td>
</tr>
<tr>
<td>4</td>
<td>1</td>
<td>1</td>
<td>-1</td>
<td>46.70</td>
</tr>
<tr>
<td>5</td>
<td>-1</td>
<td>-1</td>
<td>1</td>
<td>41.50</td>
</tr>
<tr>
<td>6</td>
<td>1</td>
<td>-1</td>
<td>1</td>
<td>66.33</td>
</tr>
<tr>
<td>7</td>
<td>-1</td>
<td>1</td>
<td>1</td>
<td>60.50</td>
</tr>
<tr>
<td>8</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>52.10</td>
</tr>
</tbody>
</table>

Processing of obtained results from Table 2 by experimental design techniques resulted in a mathematical model of accelerated composting in a drum-type bio-fermenter:

\[
Y = 57.279 + 2.088 x_1 - 2.171 x_3 - 8.913 x_1 x_2 + 2.021 x_1 x_3 + 2.246 x_2 x_3 \tag{2}
\]

Based on the calculation results the experiment reproducibility error was \( S_{repr} = 1.844 \).

The model only shows significant coefficients, which exceed \( S_{repr} \).

The model was verified on the statistical experimental data, which were obtained during the biofermenter operation [4; 11].

The model analysis revealed the two-factor interaction of \( x_1 x_2 \) (time and aeration rate factors) to have the most sizable contribution to the temperature variation \( Y \). This interaction has a completely physical meaning since it determines the amount of oxygen supplied into the reaction zone in the biofermenter. The interaction \( x_2 x_3 \) is also explainable and determines the efficiency of oxygen delivery to the microorganisms in the whole compost mass. The contribution of the remaining variables to the variation of \( Y \) is approximately the same. This conclusion fully complies with the bio-fermentation concept.

The coefficient of the constant term is exponentially higher than the other significant coefficients and, in addition, the coefficient of the two-factor interaction \( x_1 x_2 \) is greater than the other coefficients in the modulus. The theory of the experiment design states that the yield surface of the phenomenon...
under study represents “nearly stationary region” [12]. In this context, according to the theory of the experiment design it is no longer expedient or practical to conduct the steep ascent since the practical objective of the study was to find model-rational modes for two regulated temperatures of 60 and 80°C, underlying the production of qualitatively different products [13; 14].

The obtained mathematical expression (2) adequately describes the main indicator of the process, and is thus a model of the phenomenon under consideration – the temperature of the composted mass in the biofermenter. It gives a reasonable possibility to calculate the rational operation modes of the drum biofermenter. The calculation and actual results are shown in Table 3.

<table>
<thead>
<tr>
<th>Mode</th>
<th>Aeration time, min·h⁻¹</th>
<th>Aeration rate, m·s⁻¹</th>
<th>Drum rotation interval, hour</th>
<th>Temperature in bio-fermenter, °C</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>X₁</td>
<td>X₂</td>
<td>X₃</td>
<td>Y_C</td>
</tr>
<tr>
<td>I</td>
<td>9</td>
<td>5.0</td>
<td>6</td>
<td>80.19</td>
</tr>
<tr>
<td>II</td>
<td>10</td>
<td>5.0</td>
<td>12</td>
<td>82.80</td>
</tr>
<tr>
<td>III</td>
<td>10</td>
<td>5.5</td>
<td>8</td>
<td>79.41</td>
</tr>
<tr>
<td>IV</td>
<td>7</td>
<td>2.0</td>
<td>8</td>
<td>80.80</td>
</tr>
<tr>
<td>V</td>
<td>3</td>
<td>9.5</td>
<td>12</td>
<td>61.20</td>
</tr>
<tr>
<td>VI</td>
<td>3</td>
<td>8.5</td>
<td>8</td>
<td>60.06</td>
</tr>
<tr>
<td>VII</td>
<td>7</td>
<td>6.5</td>
<td>12</td>
<td>60.84</td>
</tr>
<tr>
<td>VIII</td>
<td>5</td>
<td>5.5</td>
<td>6</td>
<td>61.70</td>
</tr>
<tr>
<td>IX</td>
<td>4</td>
<td>9.5</td>
<td>12</td>
<td>59.28</td>
</tr>
</tbody>
</table>

The created model allowed to identify the rational operation modes of a drum bio-fermenter: to produce bedding – mode II (aeration time 10 min·h⁻¹; aeration rate 5 m·s⁻¹; drum rotation interval 12 hour); to produce the organic fertiliser – mode VII (aeration time 7 min·h⁻¹; aeration rate 6.5 m·s⁻¹; drum rotation interval 12 hour). The F-test statistics proved the high accuracy of the model.

The self-heating intensity of the processed material varied depending upon the applied operation mode (Fig. 2).

**Fig. 2. Self-heating process in a drum bio-fermenter:** a – mode II; b – mode VII

The analysis revealed that the required values of temperature can be achieved by various combinations of factors, which are decisive for the operating modes. For example, the desired temperature of 80 °C to produce bedding may be achieved by different values of X₃ – drum rotation interval of 6, 8 and 12 hours. However, in this case the aeration rate X₂ varies in the range of 2-5. 5 m·s⁻¹, and the aeration time X₁ varies in the range of 7 to 10 min.

The required temperature of 60 °C may be achieved at lower values of X₁, but in this case the aeration rate X₂ increases. This confirms the effect of the oxygen amount as the main indicator of the biofermentation process.
If we take the value of the variable $X_3 = 12$ hours to be rational, in this case again it is possible to achieve the desired results.

In the operation mode IV, the required temperature is achieved under the aeration rate below the minimum. Consequently, other operation modes feature the surplus amount of oxygen in the biofermenter. To clarify this phenomenon more research is needed.

**Conclusions**

1. One of the most promising technologies for utilisation of solid fraction of cattle manure is the technology of accelerated composting in a drum biofermenter. This technology allows to obtain a product with desired final properties (organic fertilizer or bedding for farm animals) in a short time and with minimal loss of nutrients.

2. A laboratory-scale model of the drum biofermenter was designed and manufactured to study and to vary the operation modes.

3. Based on the study outcomes an adequate mathematical model of accelerated composting in the drum biofermenter was created.

4. The created model allowed to select the most rational operation modes of the biofermenter to produce bedding (aeration time $10$ min·$h^{-1}$; aeration rate $5$ m·$s^{-1}$; drum rotation interval $12$ hour) and the organic fertiliser (aeration time $7$ min·$h^{-1}$; aeration rate $6.5$ m·$s^{-1}$; drum rotation interval $12$ hour).

5. To verify the obtained data it is scheduled to test the biofermenter in the production environment on a dairy farm, with the output of solid fraction of cattle manure being $18.2$ tons per day and the moisture content being $70\%$.

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